Transformation et comportement des matériaux

Materials behaviour and processing

Fractures Mechanics

Mécanique de la Rupture

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 ARTS ET MÉTIERS ParisTech – Aix en Provence

23 mars 2010



Outline

Some exemples of ruptures mechanics

The material and the design of RMS Titanic



Brittle material | Problem

A noted philanthropist offers you the chance to earn \pounds 50 000 by simply hanging from a rope for just one minute. The rope is attached to a sheet of glass which is 300 cm long by 10 cm wide and 0.127 cm thick.

Complicating the situation are:

- The glass sheet contains a central crack with a length of 1.62 cm that is orientated parallel to the ground and perpendicular to the longest side of the glass sheet. The fracture toughness of the glass is known to be 0.83 MPa.m^{1/2}.
- The rope is suspended over a deep pit containing rather annoyed green mamba snakes.

Would you try for the pot of gold at the end of the rainbow?
The stress intensity factor for a through-thickness crack is given by:

$$K=Y\sigma\sqrt{\pi a}$$
 where $Y=1+0.256\Big(rac{a}{W}\Big)-1.152\Big(rac{a}{W}\Big)^2+12.2\Big(rac{a}{W}\Big)^3$



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Fracture of the glass

Brittle material | Solution

The size of the glass sheet is necessary to calculate the stress in the sheet due to your weight hanging on the rope. Remember that this stress is calculated on the full cross-sectional area of the sheet, i.e. as though the crack is absent. This is clearly a finite sheet of glass, so we need to correct the stress intensity equation for this. Essentially:

$$K = Y \sigma \sqrt{\pi a}$$

where the finite geometry correction function Y is given by:

$$Y = 1 + 0.256 \left(\frac{a}{W}\right) - 1.152 \left(\frac{a}{W}\right)^2 + 12.2 \left(\frac{a}{W}\right)^3$$

Hence as 2a = 16.2 mm, a = 8.1 mm and W = 100 mm, which gives Y = 1.0196. The applied stress is simply obtained from:

$$\sigma = \frac{F}{A}$$
 where $F = \text{load}$ and $A = \text{cross-sectional}$ aera

i.e.
$$\sigma = \frac{60 \times 9.81}{100 \times 1.27}$$
 MPa for a 60 kg person $\rightarrow \sigma = 4.63$ MPa

Hence
$$K = 1.0196 \times 4.63 \sqrt{\pi \times 8.1 \times 10^{-3}} = 0.75 < 0.83 \text{ MPa.m}^{1/2}$$

This calculation is not based on my own weight and, if I was feeling brave, I might try to money. In general terms, the margin of safety is somewhat low - it might be better to let a vounger and lighter sibling earn the money for you!

The material and the design of RMS Titanic

The raison of sinking





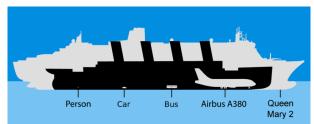
RMS Titanic before this first voyage - Iceberg



Titanic Size

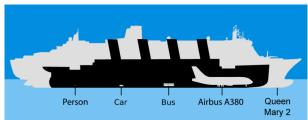
► Length 269 m

- Width 30 m
- ▶ Draft (from waterline to bottom of the hul) ≈ 11 m
- Depth (from waterline to deck) 45.5 m
- Weight 52250 :
- ► Power 33 1 MW
- ► Speed 42-45 km h⁻¹



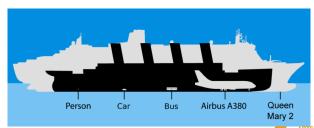


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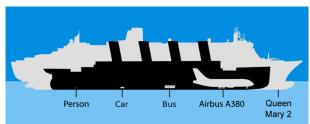
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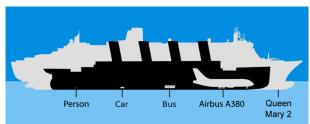
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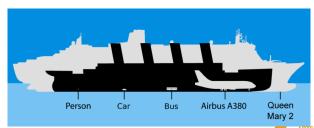
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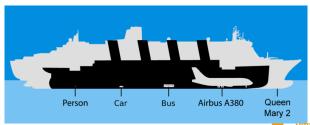
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First voyage

- ► On April 10, 1912, RMS Titanic began her voyage from Southampton
- On April 14 @ 11:20 PM RMS Titanic struck an iceberg on her right hand side of the front section facing while traveling at a speed of 20.5 knots (38 km.⁻¹)
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Titanic route

What caused Titanic to sink?



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Reasons for sinking

1. Material issues

- Composition
- ► Mioroetruotur
- ► Mechanical Properties

2. Design issues



Titanic at the bottom of the Atlantic ocean



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Titanic at the bottom of the Atlantic ocean

- 1. Material issues
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- 2. Design issues
 - Design of watertight compartments



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Titanic at the bottom of the Atlantic ocean

Material composition | Hull steels

Table: composition in weight percent [K. Felkins, H. P. Leighly, and A. Jankovic. JOM, 50(1), 1998, 12-18]

	Titanic hull plate	A36 modern structural steel
С	0.21	0.20
Mn	0.47	0.55
Р	0.045	0.012
S	0.069	0.01 to 0.04
Si	0.017	0.007
Cu	0.024	0.01
0	0.013	-
N	0.0035	0.0032
Mn :S Ratio	7 :1	15 :1 (typical)

- ► Presence of relatively high amounts of P and S embrittles the steel at low temperature
- ▶ The lower Mn :S ratio increases the ductile-brittle transition temperature



Material composition | Hull steels

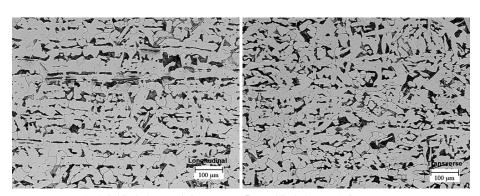
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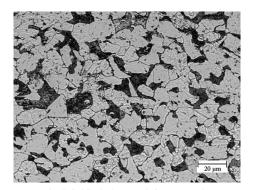
Hull steel microstructure



Longitudinal direction (average grain diameter \approx 60 μ m – Transversal direction (average grain diameter \approx 42 μ m



Modern A36 microstructure



Longitudinal direction (average grain diameter \approx 26 $\mu m)$



Effect of grain size

► How does the grain size affect strength?

- ▶ Hall-Petch equation : $\sigma_{vs} = a + bd$
- Yield strength of steel with 26 μ m grain size is about 27 % higher than that of a steel with 42 μ m grain size if the value of a is small
- ► N.A.: $\frac{\sigma_{\text{Filance}}^{\text{Tilance}}}{\sigma_{\text{A}}^{\text{A36}}} = \frac{a+b.42^{-1/2}}{a+b.20^{-1/2}} = \frac{a+6.5b}{a+5.1b}$ if $a \ll b$ then $\frac{\sigma_{\text{Filance}}^{\text{Tilance}}}{\sigma_{\text{A}}^{\text{A36}}} = \frac{6.5}{5.1} = 1.27$
- Because structures are designed with adequate factor of safety, the grain size difference did not significantly contribute to the failure.



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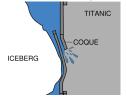
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Material failure

When the Titanic collited with iceberg, the hull steel and the wrought iron rivets failed





Collision with iceberg - The number of rivets for Titanic assembly is about 3 000 000

- The steel and the wrought iron rivets failed by brittle fracture
- Brittle facture

is a failure of a metal by rapid crack propagation and without any significant deformation





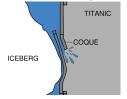
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Titanic structure was assembled



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Titanic structure was assembled using plates riveting

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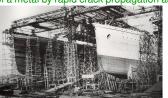
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Brittle fracture

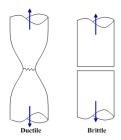
 The direction of crack motion is very nearly perpendicular tho the direction of applied tensile stress and yields relatively flat fracture surface

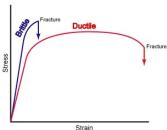




Plate riveting - Brittle crack of rivet

 Schematic representations of tensile stress-strain behavior for brittle and ductile materials loaded to fracture





Brittle fracture

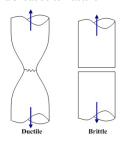
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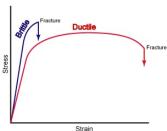




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 Schematic representations of tensile stress-strain behavior for brittle and ductile materials loaded to fracture





- What was the effect of the impact with the iceberg?
- Did the sulphur content play a role in the failure?
- What was the ductile to brittle transition temperature for the steel used to construct the hull of Titanic?
- ▶ Did the sea water temperature experienced by the Titanic (-2°C) play a role?



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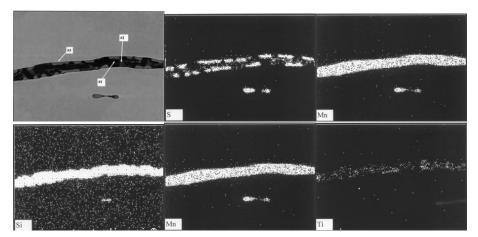
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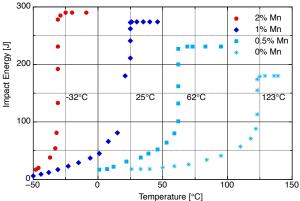
Cause of the brittle fracture | Sulphur





Cause of the brittle fracture | Effect of steel composition

 Higher %Mn is beneficial to prevent ductile to brittle transition because Mn prevents formation of brittle iron sulfides

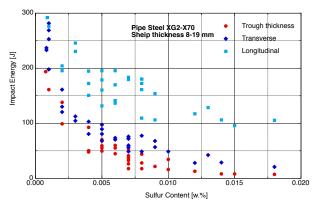


Effect of Mn composition on ductile/brittle temperature



Cause of the brittle fracture | Sulphur Effect

 Lower %S is beneficial to prevent ductile to brittle transition because S prevents formation of brittle iron sulfides



Effect of S composition on ductile/brittle temperature



Material | Tensile properties

Table: [H. P. Leighly, B. L. Bramfitt, and S. J. Lawrence. Practical Failure Analysis, 1(2), 2001]

	Titanic Steel	A36 modern steel		
Yield Strength [MPa]	193	338		
Tensile Strength [MPa]	417	441		
Total Elongation [%]	29.0	27.0		
Reduction in Aera [%]	57.1	66.0		

► Presence of relatively high amounts of P and S embrittles the steel at low temperature



Material | Charpy Impact Test

- The energy absorption is a measure of the impact energy
- The results are qualitative in nature and are useful in making comparisons
- Determine whether or not a material experiences a ductile/brittle transition with decreasing temperature and, if so, the range of temperatures over which it occur





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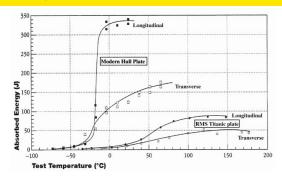
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Material | Effect of Temperature on Toughness



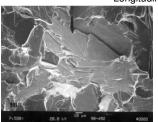
Effect on Temperature on Modern and Titanic Steel

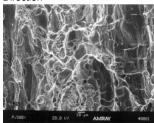
Table: [H.P. Leighly, B.L. Bramfitt and S.J. Lawrence, RMS Titanic : A metallurgical problem, Journal of Failure Analysis and Prevention, Volume 1, Number 2 / avril 2001, 10-37]

	Litanic Steel		A36 modern steel			
	Longitudinal	Transverse	Longitudinal	Transverse	1	
	Direction	Direction	Direction	Direction	İ	
Impact Energy @ -2°C [J]	4	4	325	100_	DTC	Laboratoire
Ductile-brittle Transition	30°C	42°C	-42°C	-42°C	ET MÉTIERS	MécaSurf
Temperature						ARTS & MÉTIERS Paristach
				Aix-en-Provence	-	Ed. 6496 - Innoises Carmon AATE - die en Pronsess

Material | Fracture Surface

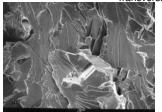
Longitudinal Direction

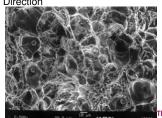




Brittle fracture @ -32°C - Ductil fracture @ 120°C

Transversal Direction



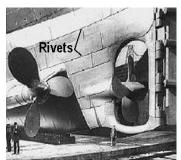




Titanic Rivet | Failure

Tremendous forces were created on impact with the iceberg

- Rivets failed either in shear or by elongation
- Rivet heads in the areas of contactcwere simply popped of
- More seams opened up
- Water was flooded the hull of the ship

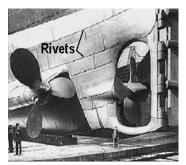


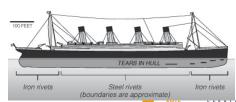




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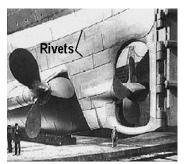
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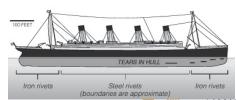






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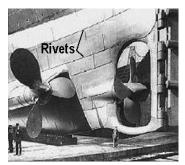


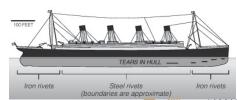




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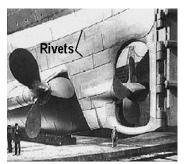






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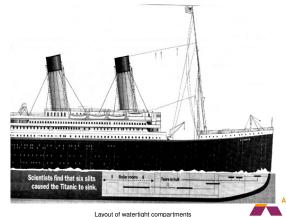


Rivets were made from wrought iron - Rivets repartition



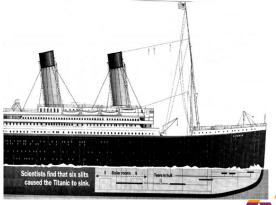
Titanic Design flaws

- Along with the material failures, poor design of the watertight compartments in the Titanic's lower section was a factor in the disaster.
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What caused Titanic sink? | Main reason of sinking

- ► The failure of the hull steel resulted from brittle fractures caused by
 - High impact loading of the collision with the iceberg
 - Low temperature water on the night of the disaster
 - High sulphur content of the stee

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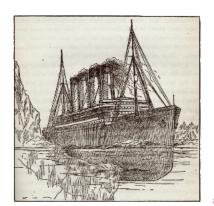


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- Mandatory use of the wireless
 - Able to receive weather reports, check their positions, and call for help in emergencies
- Increased lifeboat capacity
- Implementation of the ice patrol

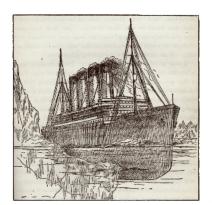




Lesson from the disaster | Safety regulations

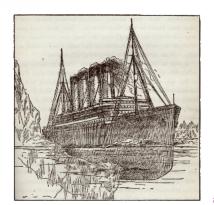
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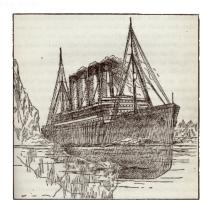


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